

Modern Control System

Non-Linear System & Linearization

1. Describe the process of linearization by small signal analysis.
2. Linearize following non-linear equation with equilibrium state $x_0=0$

$$\begin{aligned} \dot{x} &= x_2 \\ \dot{x}_2 &= \mu(1 - x^2)x_2 - x_1 \quad \mu > 0 \end{aligned}$$

Also check its stability

3. The state equation of a nonlinear system are given below. Determine all points of equilibrium and investigate the stability in the neighbourhood of these points

$$\begin{aligned} \dot{x}_1 &= x_2 \\ \dot{x}_2 &= -x_1^2 - x_2^2 - 2x_1 - 2x_2 \end{aligned}$$

4. Derive the describing function of following
 - a. Ideal relay
 - b. Practical relay
 - c. Combination of dead zone and saturation
 - d. Backlash
5. How stability is decided by describing function method?
6. Determine stability of following system by describing function method. The describing

function of nonlinearity is given by $G(x)_D = \frac{2K}{\pi} \left[\sin^{-1} \frac{s}{X} + \frac{s}{X} \sqrt{1 - \left(\frac{s}{X}\right)^2} \right]$

